

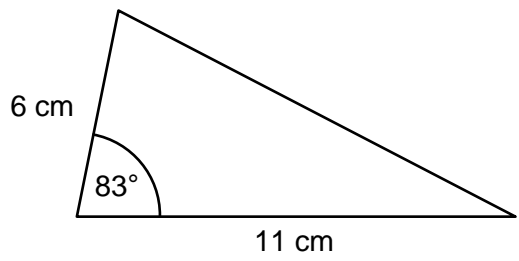


Area of a Triangle (Trigonometry)



← REVISE THIS TOPIC

1 Work out the area of the triangle.



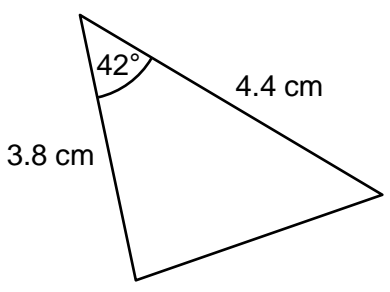
Not drawn accurately

[2 marks]

$$\frac{1}{2} \times 6 \times 11 \times \sin(83)$$

Answer 32.8 cm²

2 Work out the area of the triangle.



Not drawn accurately

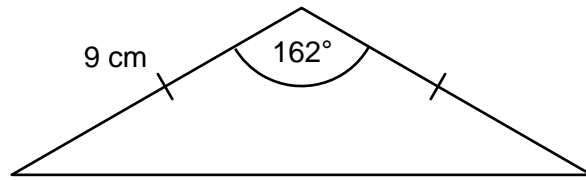
[2 marks]

$$\frac{1}{2} \times 3.8 \times 4.4 \times \sin(42)$$

Answer 5.6 cm²



3 Work out the area of the triangle.



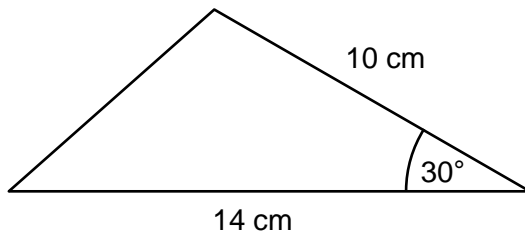
Not drawn accurately

[2 marks]

$$\frac{1}{2} \times 9 \times 9 \times \sin(162)$$

Answer 12.5 cm²

4 Work out the area of the triangle.



Not drawn accurately



[3 marks]

$$\frac{1}{2} \times 10 \times 14 \times \sin(30)$$

$$= \frac{1}{2} \times 10 \times 14 \times \frac{1}{2}$$

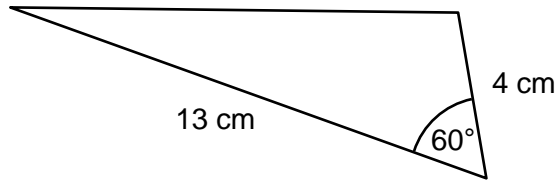
$$= 5 \times 7$$

Answer 35 cm²



5

Work out the area of the triangle.

Give your answer in the form $k\sqrt{3}$, where k is an integer.

Not drawn accurately



[3 marks]

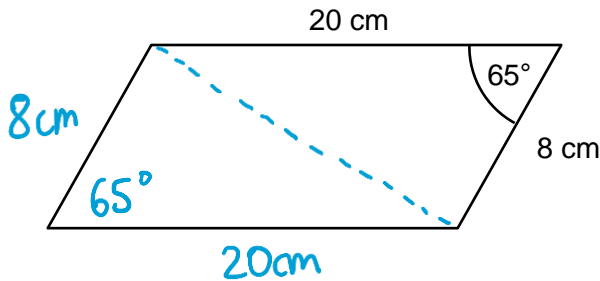
$$\frac{1}{2} \times 4 \times 13 \times \sin(60)$$
$$= \frac{1}{2} \times 4 \times 13 \times \frac{\sqrt{3}}{2}$$

$$= \frac{52\sqrt{3}}{4}$$

Answer 13√3 cm²

6

Work out the area of the parallelogram.



Not drawn accurately

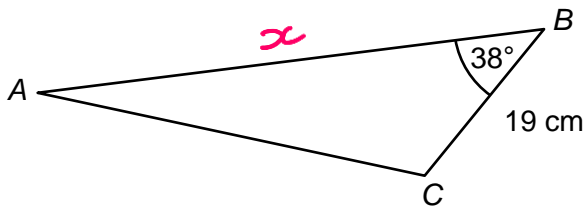
[3 marks]

$$\frac{1}{2} \times 20 \times 8 \times \sin(65) = 72.50462296$$

$$72.50462296 \times 2 = 145.0092459$$

Answer 145.0 cm²

7 The area of triangle ABC is 350 cm^2



Not drawn accurately

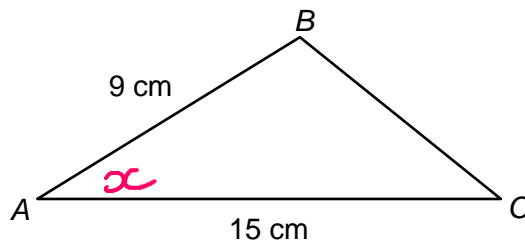
Work out the length of AB .

[3 marks]

$$\begin{aligned} \times 2 \quad \left(\frac{1}{2} \times 19 \times x \times \sin(38) = 350 \right) \times 2 \\ 19 \sin(38) x = 700 \\ x = \frac{700}{19 \sin(38)} \end{aligned}$$

Answer 59.8 cm

8 The area of triangle ABC is 23 cm^2



Not drawn accurately

Work out the size of the acute angle, BAC .

[3 marks]

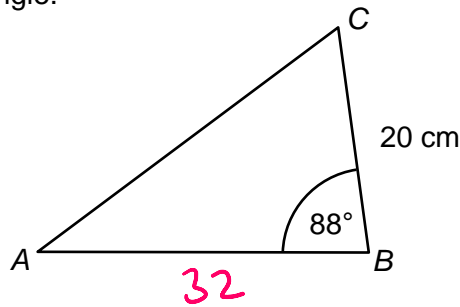
$$\begin{aligned} \times 2 \quad \left(\frac{1}{2} \times 9 \times 15 \times \sin(x) = 23 \right) \times 2 \\ 135 \sin(x) = 46 \\ \sin(x) = \frac{46}{135} \end{aligned}$$

$$x = \sin^{-1}\left(\frac{46}{135}\right)$$

Answer 19.9 °



9 ABC is a triangle.



Not drawn accurately

$AB : BC = 8 : 5$

Work out the area of triangle ABC .

[3 marks]

$$20 \div 5 = 4$$

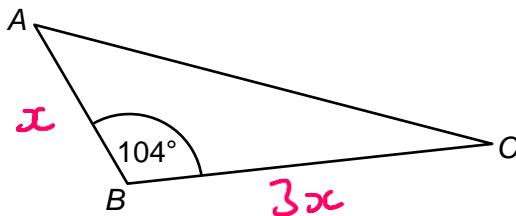
$$8 \times 4 = 32$$

$$\frac{1}{2} \times 20 \times 32 \times \sin(88)$$

$$319.8$$

Answer _____ cm²

10 ABC is a triangle.



Not drawn accurately

$AB : BC = 1 : 3$

The area of triangle ABC is 123 cm^2

Work out the length of AB .

[3 marks]

$$\frac{1}{2} \times x \times 3x \times \sin(104) = 123$$

$$3x^2 \sin(104) = 246$$

$$x^2 = \frac{246}{3 \sin(104)}$$

$$x = \sqrt{\frac{246}{3 \sin(104)}}$$

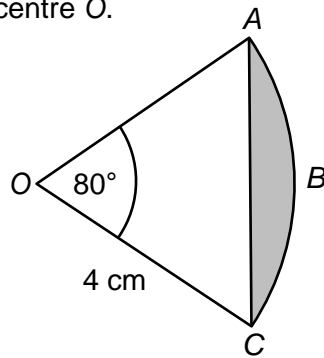
$$9.2$$

Answer _____ cm



Turn over ►

- 11 $OABC$ is a sector with centre O .



Not drawn accurately

Calculate the area of the shaded region.

[4 marks]

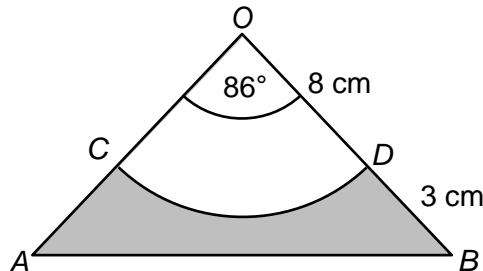
$$\begin{aligned} \text{Area of sector} &= \frac{80}{360} \times \pi \times 4^2 \\ &= 11.17010721 \end{aligned}$$

$$\begin{aligned} \text{Area of triangle} &= \frac{1}{2} \times 4 \times 4 \times \sin(80) \\ &= 7.878462024 \end{aligned}$$

$$11.17\dots - 7.87\dots$$

Answer 3.3 cm²

- 12 AOB is an isosceles triangle with $OA = OB$
 COD is a sector, centre O .



Work out the area of the shaded region.

[4 marks]

$$\begin{aligned} \text{Area of triangle} &= \frac{1}{2} \times 11 \times 11 \times \sin(86) \\ &= 60.35262504 \end{aligned}$$

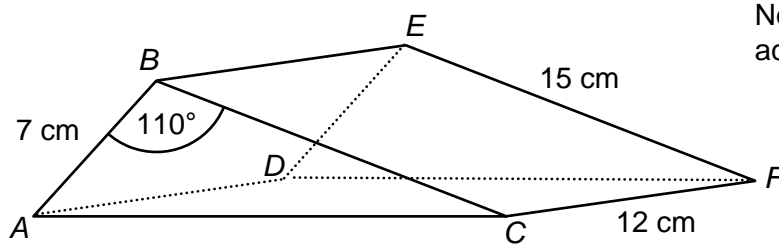
$$\begin{aligned} \text{Area of sector} &= \frac{86}{360} \times \pi \times 3^2 \\ &= 48.03146101 \end{aligned}$$

$$60.35\dots - 48.03\dots$$

Answer 12.3 cm²



13

 $ABCDEF$ is a triangular prism.

Not drawn accurately

The prism has a mass of 0.5 kg.
Calculate the density of the prism in g/cm^3
Give your answer to 3 significant figures.

[5 marks]

$$\text{Area of triangle} = \frac{1}{2} \times 7 \times 15 \times \sin(110)$$
$$= 49.33386259$$

$$\text{Volume of prism} = 49.3... \times 12$$
$$= 592.0063511$$

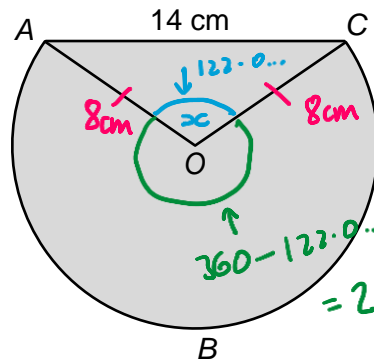
$$\text{Density} = \frac{500\text{g}}{592.0... \text{cm}^3}$$

$$= 0.8445855337 \text{g/cm}^3$$

Answer 0.845 g/cm^3 

14

ABCO is a sector with centre O.



Not drawn accurately

The perimeter of triangle AOC is 30 cm.
Calculate the shaded area.

[6 marks]

$$30 - 14 = 16 \quad 16 \div 2 = 8$$

$$\cos(x) = \frac{8^2 + 8^2 - 14^2}{2 \times 8 \times 8}$$

$$\cos(x) = -0.53125$$

$$x = \cos^{-1}(-0.53125)$$

$$x = 122.0899513$$

$$\begin{aligned} \text{Area of triangle} &= \frac{1}{2} \times 8 \times 8 \times \sin(122.0\dots) \\ &= 27.11088342 \end{aligned}$$

$$\begin{aligned} \text{Area of sector} &= \frac{237.9\dots}{360} \times \pi \times 8^2 \\ &= 132.8740376 \end{aligned}$$

$$27.11\dots + 132.87\dots = 159.984921$$

Answer 160.0 cm²

